
A note on extreme points of X^∞ -smooth balls in polyhedral spaces

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Morris proved that every separable Banach space X that contains an isomorphic copy of c_0 has an equivalent strictly convex norm such that all points of its unit sphere S_X are unpreserved extreme, i.e., they are no longer extreme points of $B_{X^{**}}$. We use a result of Hájek to prove that any separable infinite-dimensional polyhedral Banach space has an equivalent C^∞ -smooth and strictly convex norm with the same property as in Morris' result. We additionally show that no point on the sphere of a C^2 -smooth equivalent norm on a polyhedral infinite-dimensional space can be strongly extreme, i.e., there is no point x on the sphere for which a sequence (h_n) in X with $\|h_n\| \not\rightarrow 0$ exists such that $\|x \pm h_n\| \rightarrow 1$.

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